

A comparison of extended electricity price models considering the impact of wind energy feed-in

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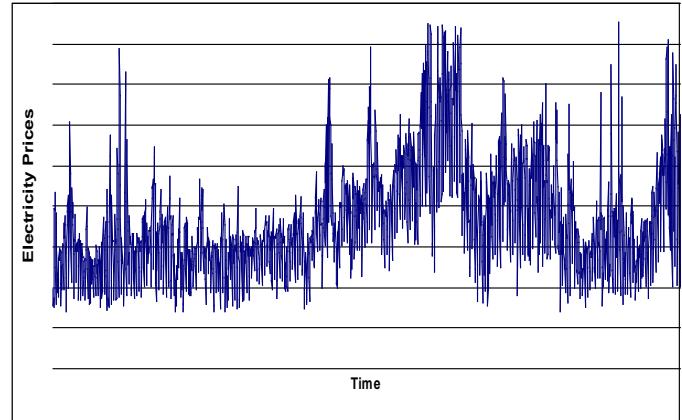
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- 1. Background**
- 2. Impact of wind power feed-in on electricity prices**
- 3. Modelling electricity prices via stochastic processes**
- 4. Simulation of wind-power feed-in**
- 5. Extended electricity price modeling considering the impact of wind power feed-in**
- 6. Conclusions and Outlook**

Background

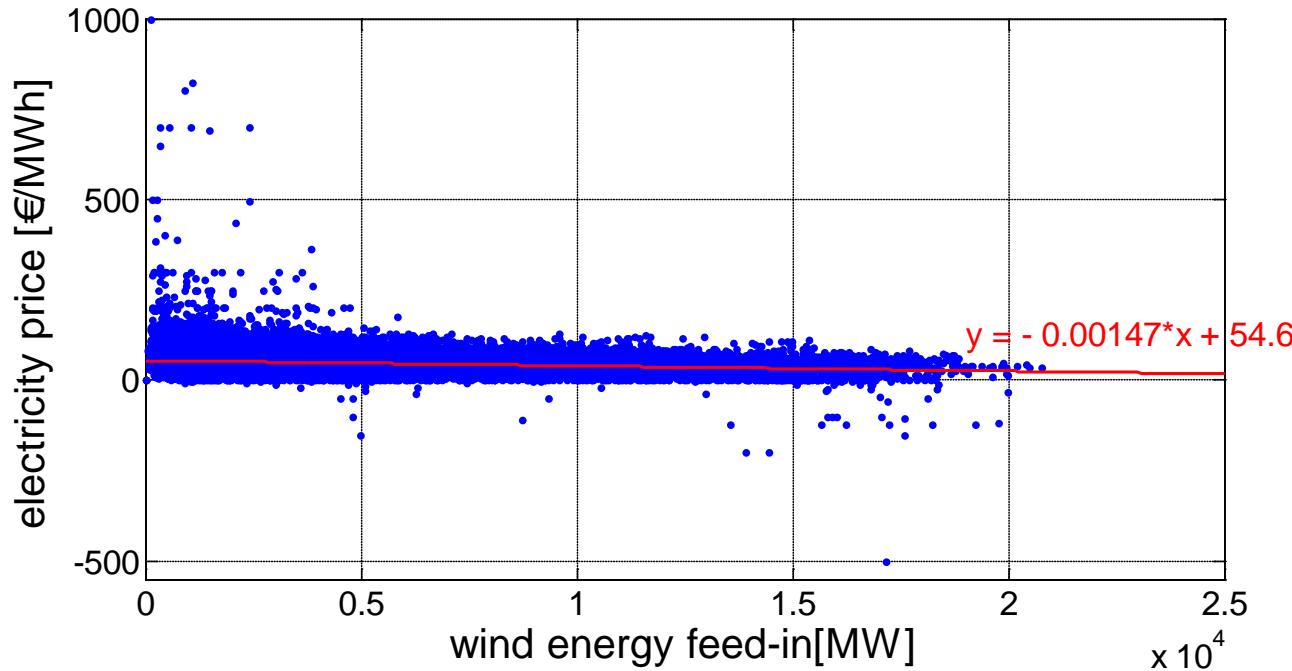
- High uncertainties in energy markets due to liberalization and structural changes
 - Electricity prices have become very volatile
- **Stochastic simulation to capture these volatilities**



- Volatile feed-in of large amount wind power into grid
 - Wind power feed-in (WPF) has a significant impact on the electricity price
 - Long-term effects on power plant mix
- Evaluation of new investments need to consider uncertain prices and WPF
- Therefore a basic knowledge of the interrelations is necessary

Impact of wind power feed-in (WPF) on electricity prices

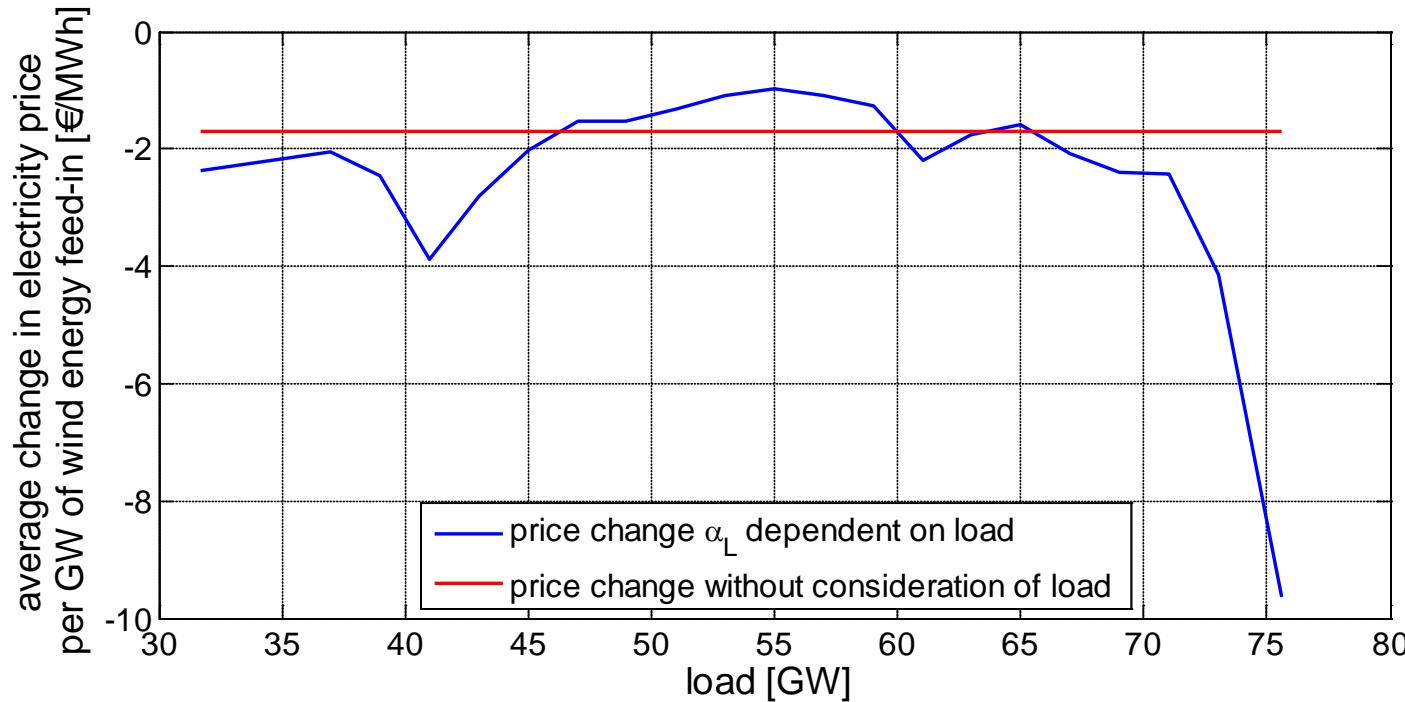
- historical couples of electricity prices and WPF (2006-2009)



- the electricity price declines by 1,47 €/MWh on an average per Gigawatt wind power feed-in
- reason: merit order effect of WPF
- the average price reduction of 1,47 €/MWh per GW does not explain extreme price decreases of up to -500€/MWh

Impact of wind power feed-in (WPF) on electricity prices

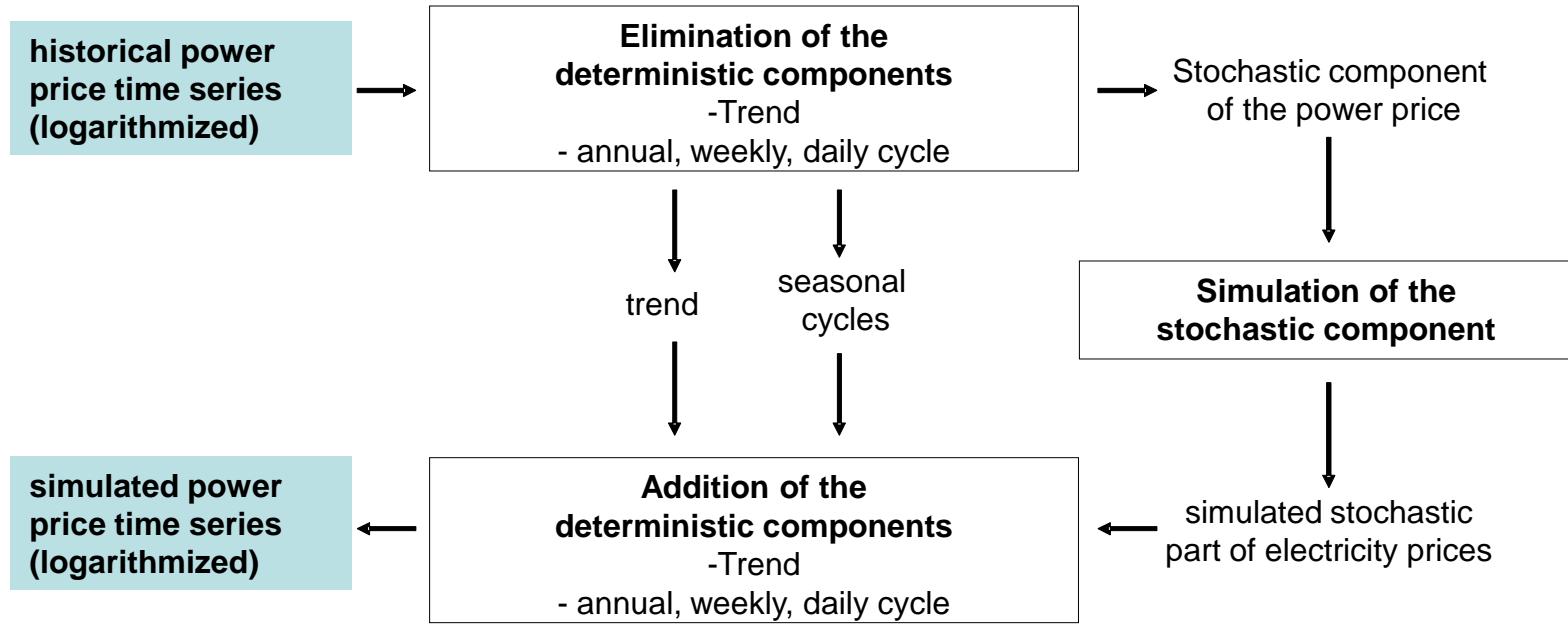
- change of electricity prices depending on the current load



- the average price change caused by WPF varies according to the demand level
- possible cause: irregular structure of the merit order curve

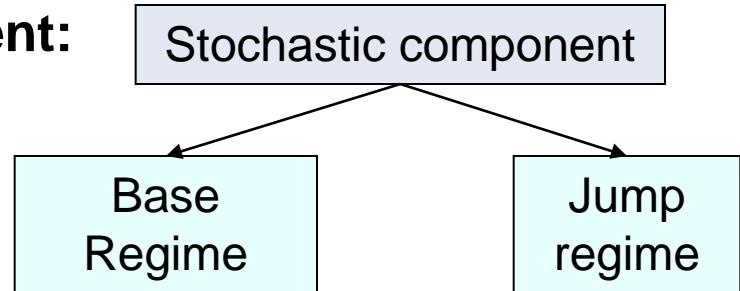
Modeling electricity prices via stochastic prices

- basic model for power price simulation:



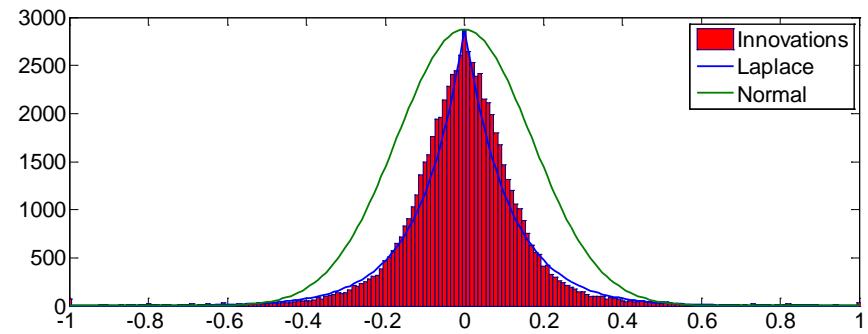
- Division of the power price into a deterministic and a stochastic components
- Simulation of the stochastic portion via models of financial mathematics

Modelling of the stochastic component:



Base regime:

- Autoregressive mean-average (ARMA(p,q))- process
 - Assumption: Price X_t^s depend on the last p prices and X_{t-p} and q innovations ε_{t-p}
$$X_t^{BASE,s} = \sum_{i=1}^p \alpha_i X_{t-i}^R + \sum_{j=1}^q \beta_j \varepsilon_{t-j} + \varepsilon_t$$
 - Parameters are estimated via MLE (Garch-Toolbox in MATLAB)
 - Innovations: $\varepsilon_t \sim \text{Laplace}(\mu_\varepsilon, b_\varepsilon)$
- Integrated ARMA (ARIMA)-process
- GARCH-Process
- Mean-Reversion process



Jump regime: extension of the base processes

$$X_t^{s,JUMP} = X_t^{s,BASE} + \ln J_t \quad \ln J_t \sim N(\mu_{\ln J}, \sigma_{\ln J}^2)$$

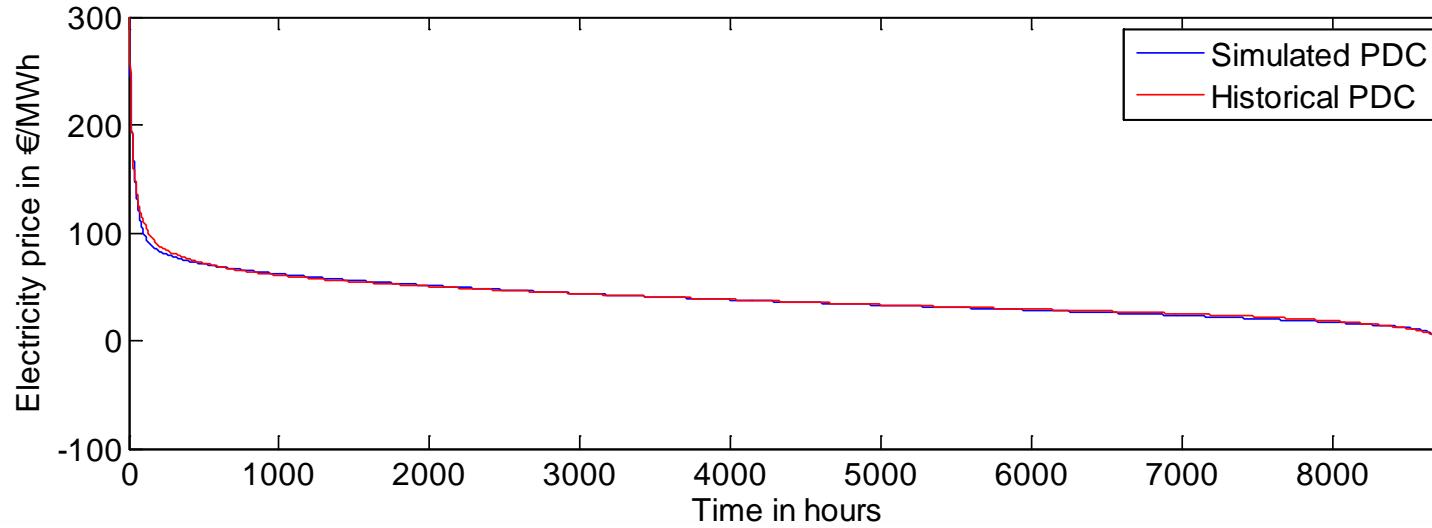
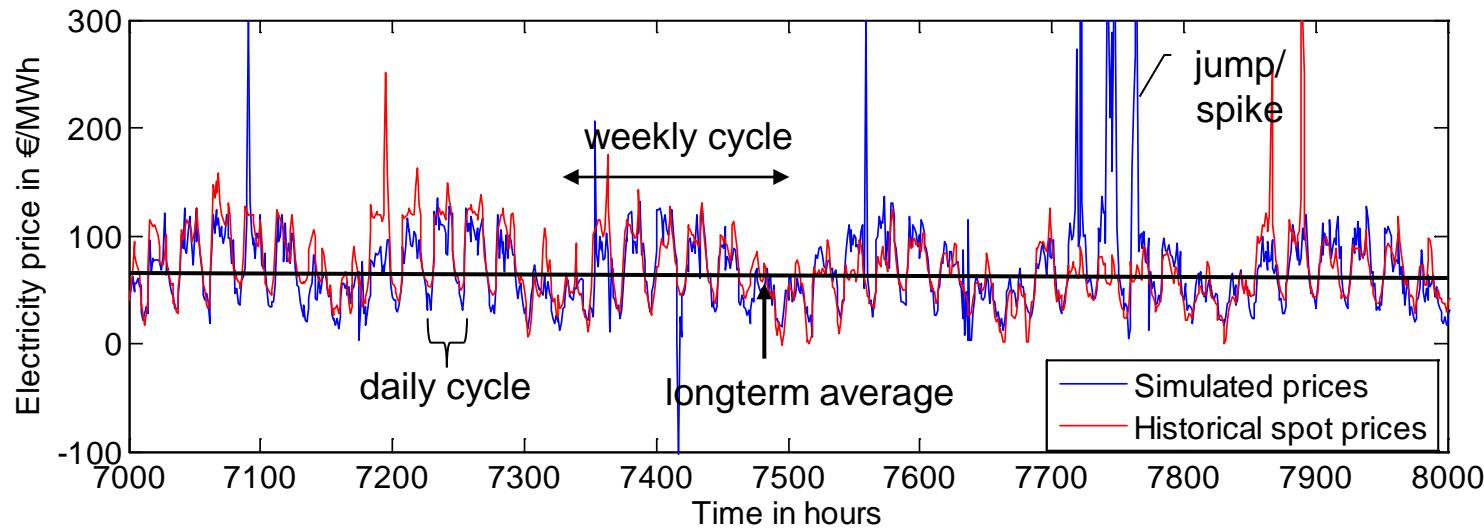
- Prices in X_t^s beyond a confidence interval $[\mu - 3 \cdot \sigma, \mu + 3 \cdot \sigma]$ are declared as jumps
- Calculation of switching probabilities as the relative frequency of price switches between the one in and out the confidence interval:

$$P_{12} = \frac{\text{card}\{l \mid X_{l,t}^{SR} \in [\mu - 3\sigma, \mu + 3\sigma] \wedge X_{l,t+1}^{SR} \in (\mu + 3\sigma, \ln 3000]\}}{\text{card}\{l \mid X_{l,t}^{SR} \in [\mu - 3\sigma, \mu + 3\sigma]\}} \quad T = \begin{bmatrix} p_{11} & p_{12} \\ p_{21} & p_{22} \end{bmatrix}$$

- Differentiation of switching probabilities for summer weekdays, winter weekdays and weekends
- *Simulation of the stochastic component X_t^s with the regime-switching model and addition of the deterministic ones*

→ Simulated electricity price paths

Modeling electricity prices via stochastic prices – simulation results



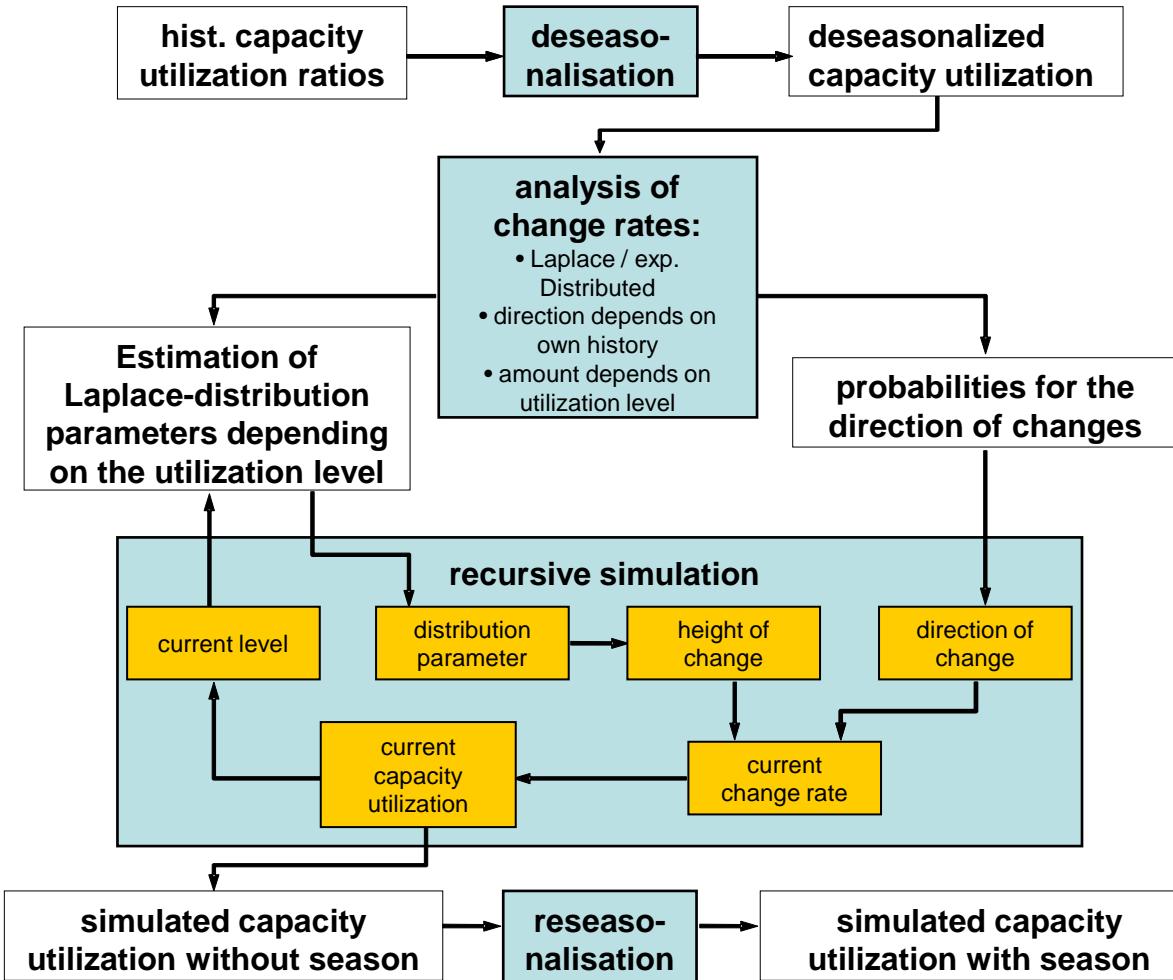
Modeling electricity prices via stochastic prices

– simulation results

Stochastic Model	MRSE [€MWh]			R2		
	2009	2008	2002-2008	2009	2008	2002-2008
Mean-Reversion (MR)	8.51	6.11	2.40	37%	52.53%	20.98%
ARMA(1,1), *(5,5)	8.63, 8.62	6.86, 7.12	2.73, 2.77	30.97%, 31.24%	43.93%, 44.70%	18.67%, 18.83%
ARIMA(1,1,1), *(5,1,5)	8.15, 8.19	5.91, 5.55	2.70, 2.64	33.21%, 33.02%	47.05%, 50.25%	19.41%, 20.18%
GARCH(1,1),*(5,5)	15.10, 17.85	9.03, 11.07	3.21, 4.18	13.57%, 10.03%	34.69%, 31.88%	13.48%, 12.53%
MR without RS	19.92	17.52	6.39	18.90%	31.49%	26.93%
GARCH without RS	109.18, 111.84	102.01, 102.97	47.12, 49.23	1.47%, 1.36%	3.89%, 3.63%	1.89%, 1.84%
ARIMA without deseasonalizing	9.94, 21.96	14.92, 13.00	9.95, 609.30	0.21%, 2.67%	0.13%, 0.11%	3.00%, 1.45%

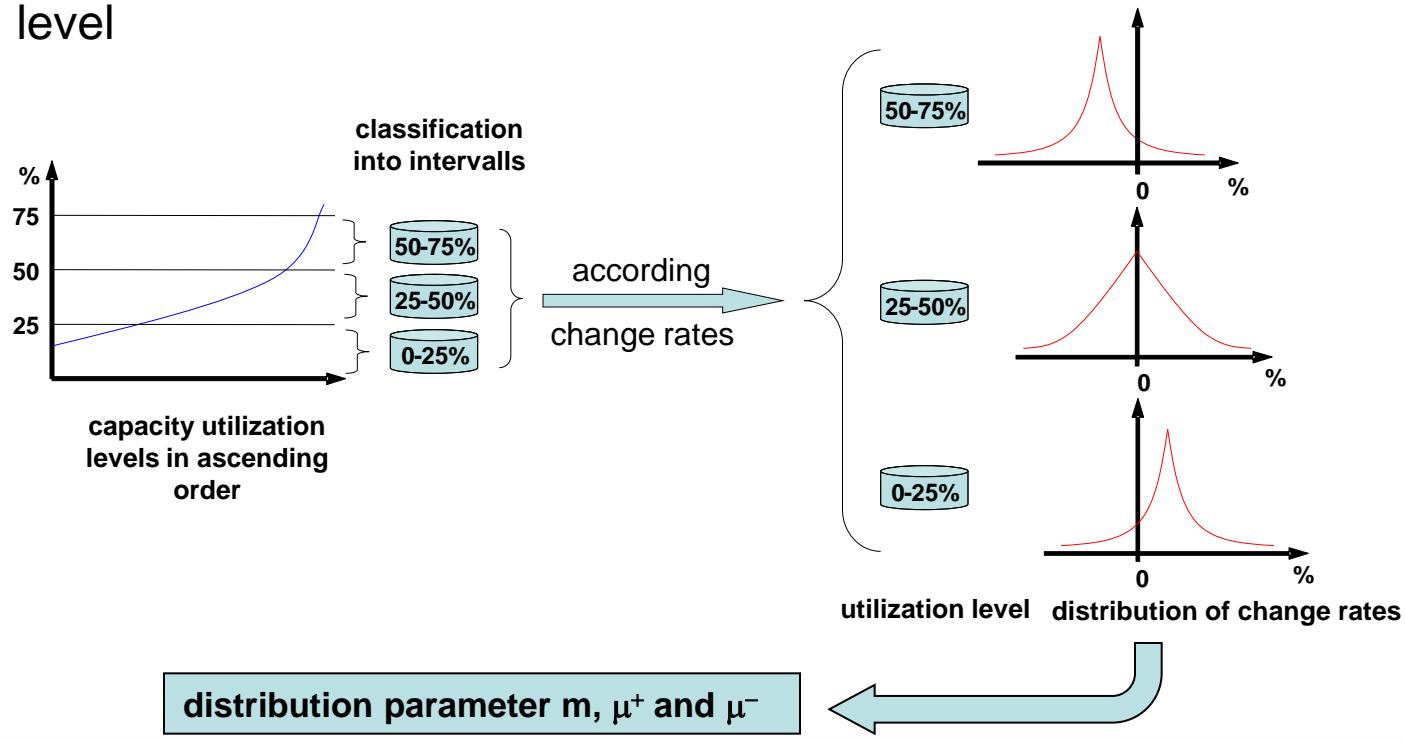
Simulation of wind power feed-in

- Overview of the simulation model



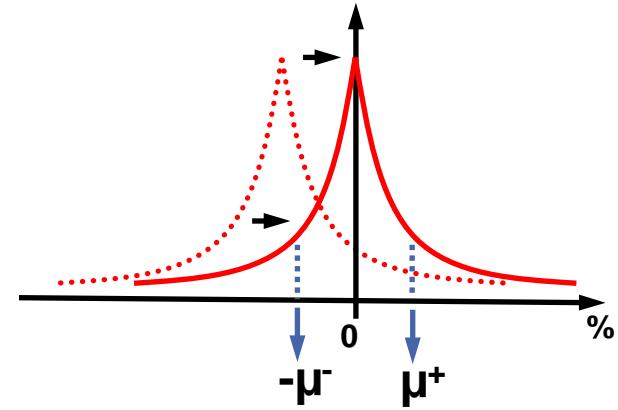
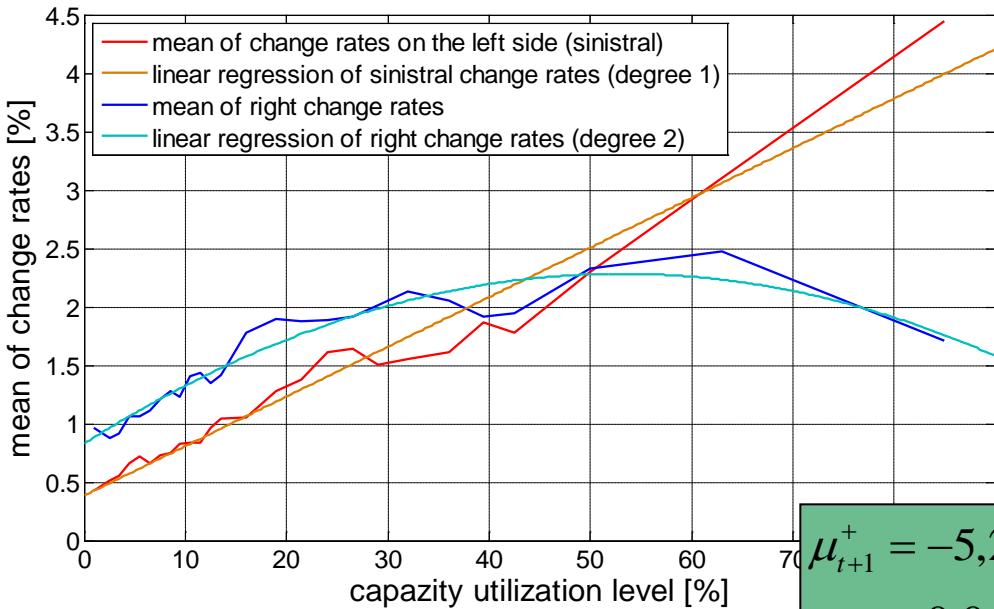
Simulation of wind energy feed-in (WEF)

- utilization levels are classified by height
- the distribution of change rates is analysed separately for each class and parameters are determined
- with the help of these distribution parameters the height of the change is determined as a random number dependent on the recent utilization level



Simulation of wind energy feed-in (WEF)

- parameters $\mu+$ und $\mu-$



$$\mu_{t+1}^+ = -5,2 \cdot 10^{-4} \cdot Niv(X_t)^2 + 0,055 \cdot Niv(X_t) + 0,83$$
$$\mu_{t+1}^- = 0,042 \cdot Niv(X_t) + 0,38$$

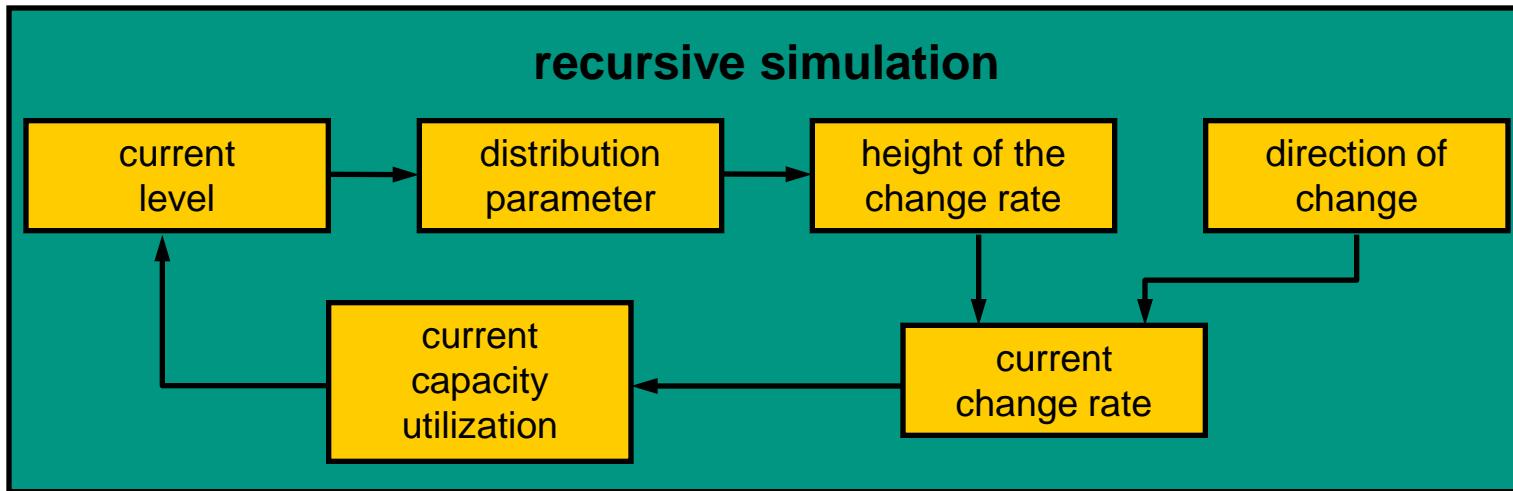
- $\mu+$ and $\mu-$ correspond to the mean of the positive and negative changes, that were moved by the modal value
- the height of negative change rates grows with increasing utilization level
- the height of positive change rates reaches its maximum at medium utilization rates

Simulation of wind energy feed-in (WEF)

- Simulation approach

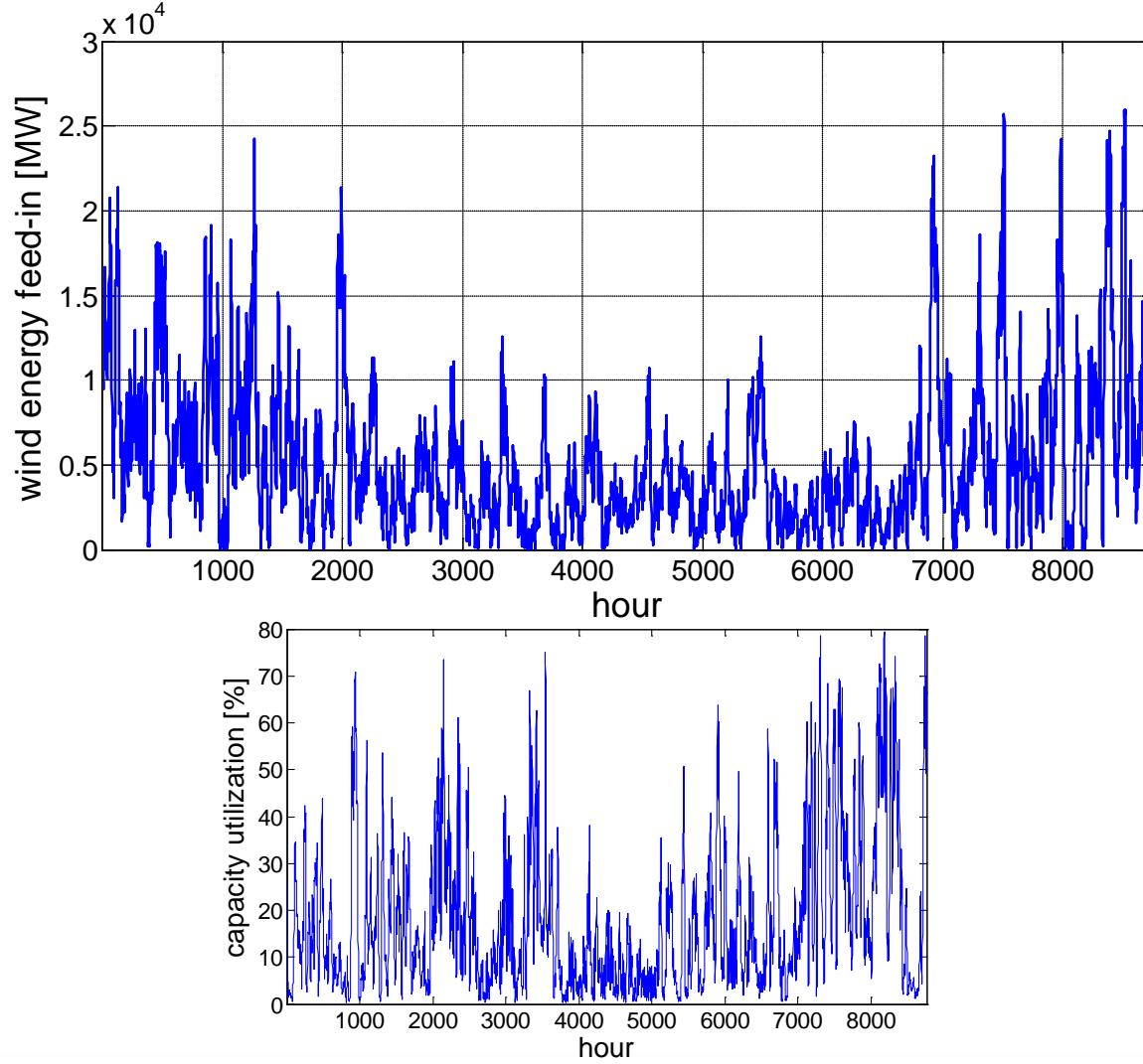
→ Recursive simulation of the hourly capacity utilization X_t^{sim} based on the model of the change rates ΔX_t^{sim}

$$X_t^{\text{sim}} = X_{t-1}^{\text{sim}} + \Delta X_{t-1}^{\text{sim}}$$



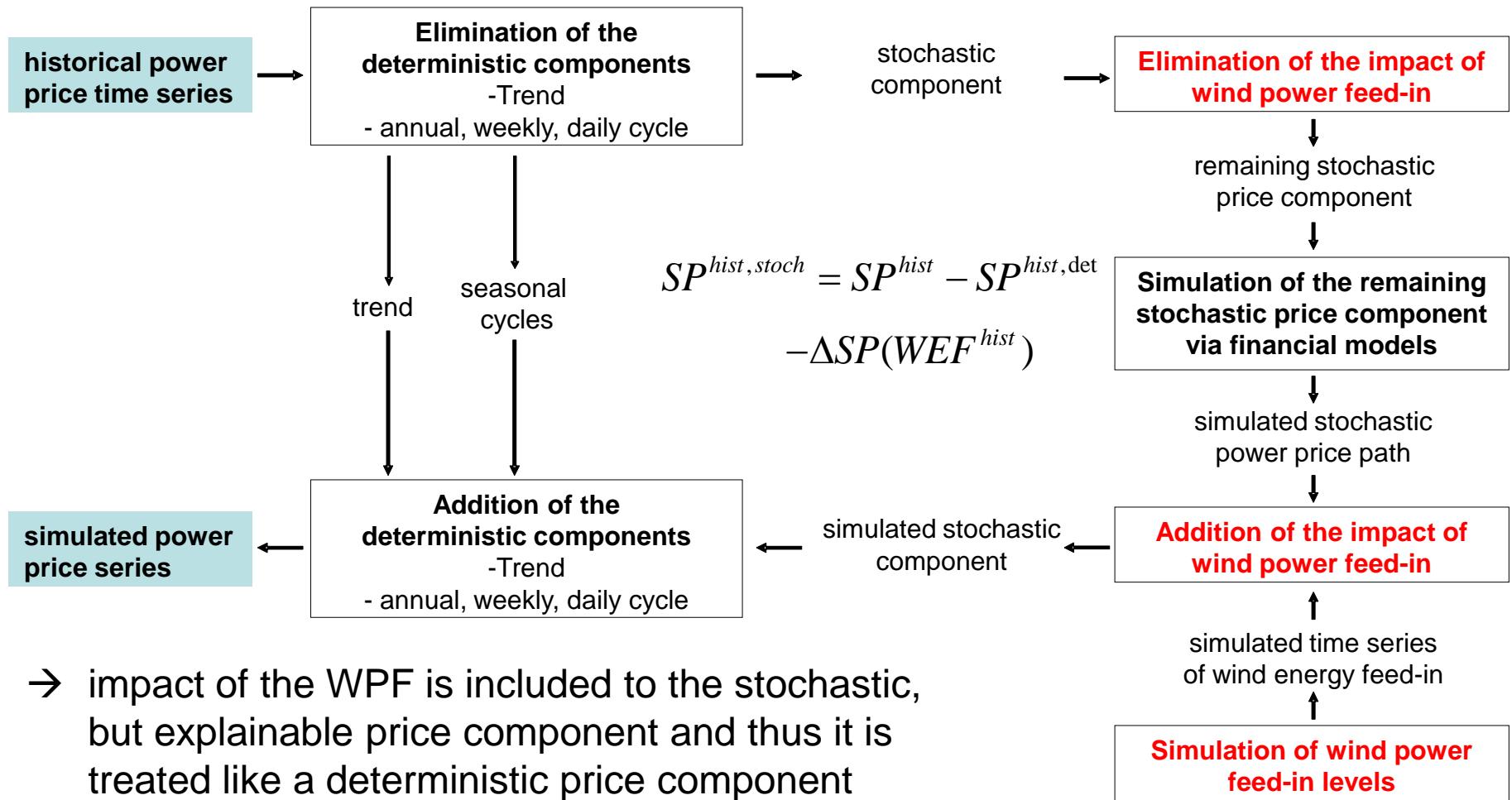
Simulation of wind power feed-in (WPF)

- Simulation results for an actual installed capacity of 26 GW wind power



Extended modeling of power prices including the impact of wind power feed-in

- extension of the base model



Comparison of the electricity price simulation results **without** and **with** consideration of wind power simulation:

	2009			2008		
	W/O Wind	with Wind	HISTORICAL	W/O Wind	with Wind	HISTORICAL
MRSE [€/MWh]	8.51	6.67	-	6.11	5.57	-
MAPE	13.93%	10.64%	-	6.40%	4.98%	-
R2	36.60%	38.38%	-	52.53%	54.80%	-
Mean [€/MWh]	41.25	38.86	38.85	67.65	65.73	65.76
σ [€/MWh]	23.94	20.16	19.41	33.87	26.02	28.66
skewness	1.49	-1.16	-3.23	2.01	0.01	1.16
kurtosis	20.08	8.66	83.90	37.85	3.42	11.84

→ the consideration of the impact of wind power leads to significant improvement of the price simulation

Summary

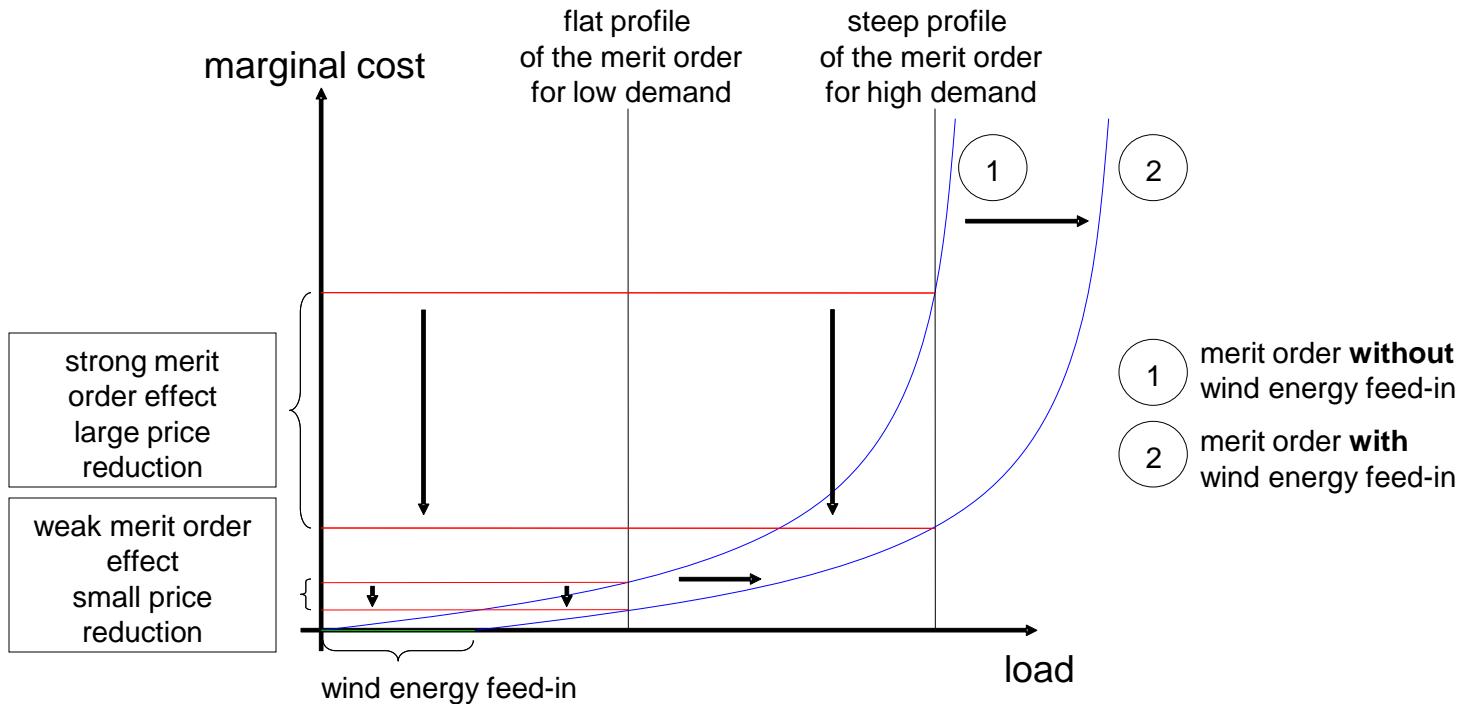
- The simulation results of the mean-reversion and the ARMA-models do not differ significantly, both models are suitable for electricity price simulation
- However, the GARCH approach is less suitable, the MRSE is very high in this case
- Regime switching approach improves the simulation immensely, the error is reduced by more than half
- Consideration of the seasonal components leads also to a significant improvement of the electricity price simulation
- Impact of wind power:
 - Depends strongly on the actual load level
 - Wind power feed-in can be simulated via Laplace-distributed change rates
 - The separation of the stochastic component into a “wind power driven” one and remaining stochastic one improves also the electricity price simulation

Thank you!

Questions?

Impact of wind energy feed-in (WEF) on electricity prices

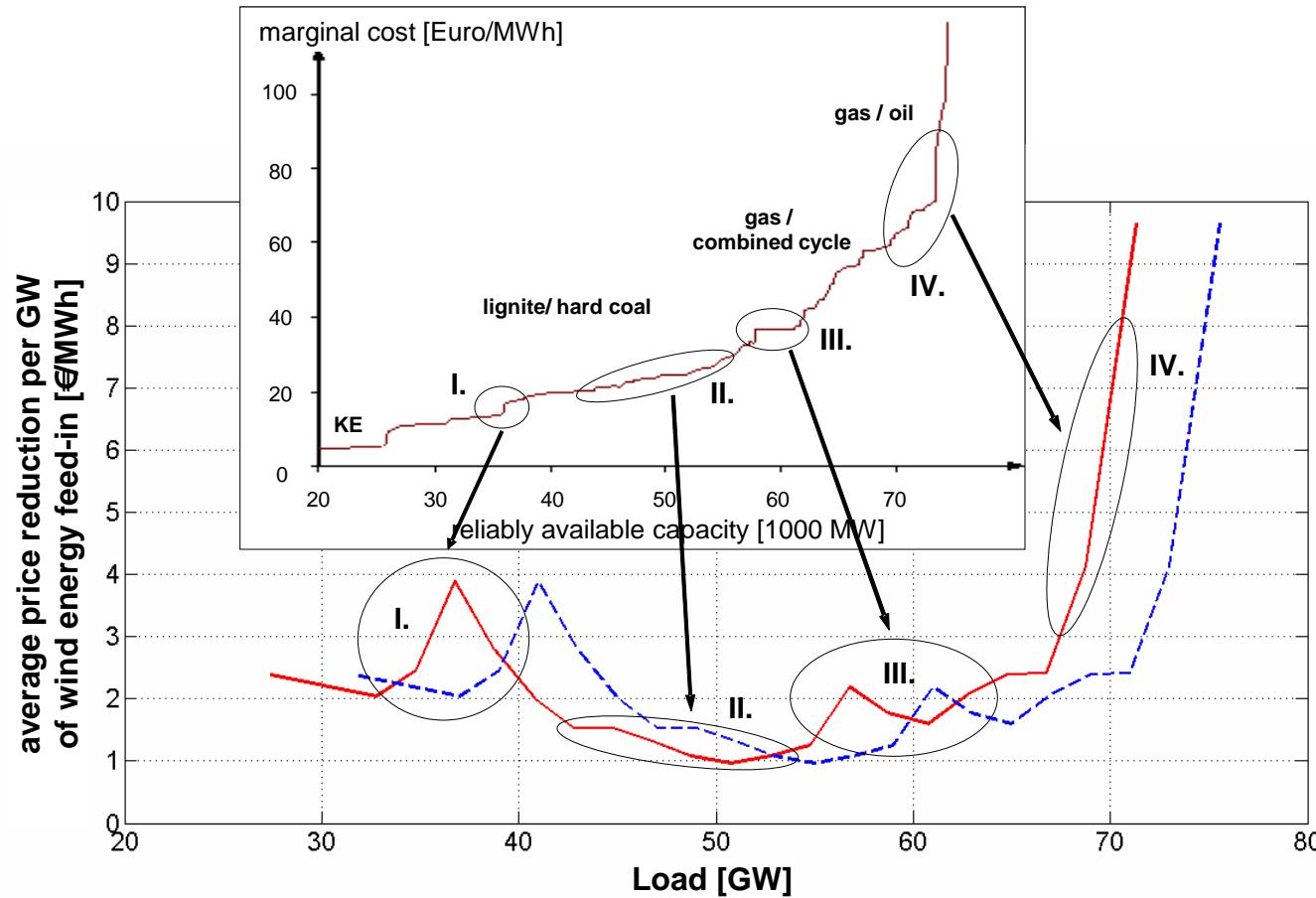
- structure of the merit order



- exponential structure, jumps and constant levels
- depending on merit order characteristics equal WEF can cause different price reductions

Impact of wind energy feed-in (WEF) on electricity prices

- Comparison of the merit order structure and price reductions



→ merit order structure and extreme market situations explain fluctuations within price reductions by WEF

Modeling of the deterministic parts:

Logarithmised prices
(2002 - 2009)

$$X_t = \ln p_t$$

- Negative prices are set to 0.01€/MWh
- Log. leads to variance stabilization

Trend of price logs

$$X_t^{trend} = X_0 + \lambda \cdot t$$

Annual cycle

$$X_{dh}^{\text{annual cycle}}(t) = \alpha_{dh} + \beta_{dh} \cos\left(2\pi \frac{t-\tau}{8760}\right) + \gamma_{dh} \sin\left(2\pi \frac{t-\tau}{8760}\right)$$

Weekly cycle

$$X_t^{\text{weekly cycle}} = \alpha + \beta \left| \sin\left(\frac{\pi \cdot t}{168} - \varphi\right) \right|$$

Daily cycle

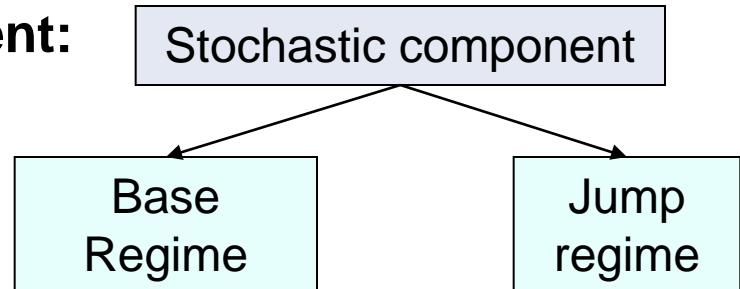
$$X_{i,\text{season}}^{\text{daily cycle}} = \frac{24}{T} \sum_{t=0}^{(T/24)-1} X_{i+24t,\text{season}}$$

$$\forall i \in \{1, 2, \dots, 24\} \wedge \forall \text{season} \in \{\text{winter}, \text{spring}, \text{summer}, \text{autumn}\}$$

Stochastic residues

$$X_t^s = X_t - X_t^{trend} - X_t^{\text{annual cycle}} - X_t^{\text{weekly cycle}} - X_t^{\text{daily cycle}}$$

Modelling of the stochastic component:



Base regime:

Mean-reversion process

- Assumption: prices return to the long-term mean μ *with the speed κ*

$$dX_t = \kappa(\mu - X_t) \cdot dt + \sigma \cdot dW_t$$

- Wiener Process $dW_t = \varepsilon_t dt^{1/2}$, whereas ε_t is a standard normally distributed error term
- Exact solution: $E(X_t) = ae^{-\theta t} + \mu(1 - e^{-\theta t})$ $\text{Cov}(X_s, X_t) = \frac{\sigma^2}{2\theta} (e^{-\theta|s-t|} - e^{-\theta(s+t)})$.

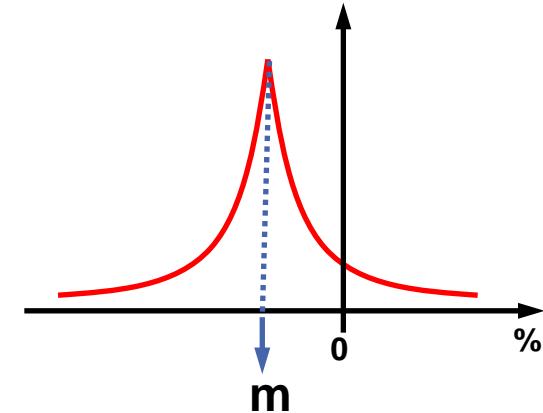
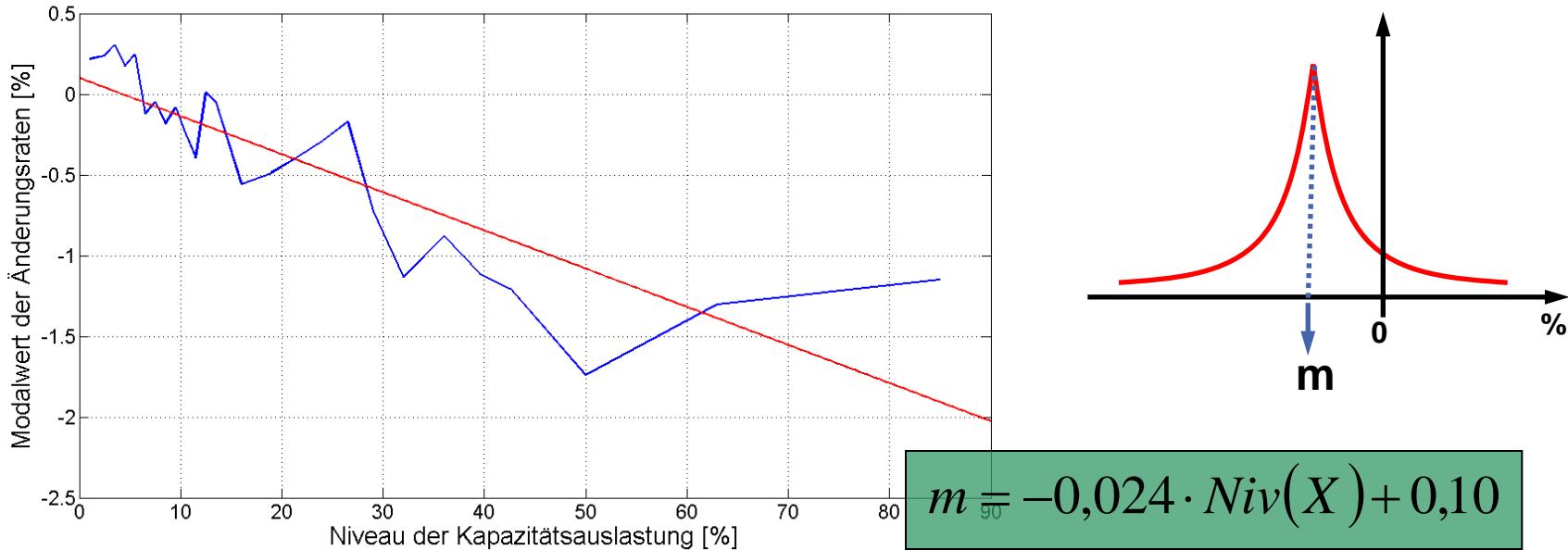
$$X_t \sim \mathcal{N}\left(ae^{-\theta t} + \mu(1 - e^{-\theta t}), \frac{\sigma^2}{2\theta}(1 - e^{-2\theta t})\right)$$

- Parameter estimation via MLE

- Analysis of change rates: dependencies
 - Dependency of change rates on historical values (Autocorrelation):
 - Direction of a change depends on previous change
 - Probability, that change will be positive or negative, results from how many directly preceding changes were positive or negative
 - With historical data probabilities can be determined and thus for each hour in the simulation time frame the direction can be provided
 - Dependency of change rates on historical values of capacity utilization:
 - historical capacity utilization determine the amount of the following change
 - this history is described by the level of utilization, defined as the moving average of the past 11 hours

Simulation of wind energy feed-in (WEF)

- parameter m



- m corresponds to the mode of change rates
- the higher the utilization level, the smaller (or more negative) the average change amount

Simulation of wind energy feed-in (WEF)

- Modelling the change rates Δx_t^{sim}

$$\Delta X_t^{\text{sim}} = \begin{cases} e_t + m_t & , l_t = 1 \\ -e_t + m_t & , l_t = -1 \end{cases}$$

$$e_t \sim \begin{cases} \text{Exp}(\mu_t^+) & , l_t = 1 \\ \text{Exp}(\mu_t^-) & , l_t = -1 \end{cases}$$

$$m_t, \mu_t^+, \mu_t^- = f[Niv_t(X_t)]$$
$$t = 1, \dots, N^{\text{sim}}$$

- Amount of the change rate is generated with a exponentially distributed random number, that is moved by the modal value of the original Laplace distribution
- The direction of the change is determined by the series I of algebraic signs, that provides the direction of the change in each hour t